Decomposition based Color Image Restoration

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Abstract— Image decomposition is widely used technique to process the given grey or color image. Need of image restoration, in general, arises when the image is noisy or blurred. This paper addresses the issue of formulation of problem associated with the image restoration based on image decomposition. Along with this, the possible proposed approach is discussed. This paper is useful for the beginners in the image decomposition and image restoration.

Index Terms—Image Decomposition, Image Restoration, Noisy Image, Image Filtering.

I. INTRODUCTION

Image restoration is required to restore the transmitted image or to recover the clear image from the distorted image. Image decomposition is the technique where the image is divided into different part or component to have the content of the image in different formats. While doing the decomposition, the properties of the image are preserved. This paper presents the formulation and the proposed approach for the image. Firstly, the problem is formulated, and along with this the proposed approach is presented where one can explore different techniques to devise the proper mechanism for the image decomposition and restoration.

This paper is organized as follows. Section II discusses the related work; problem formulation and possible proposed approach is discussed in section III. Conclusion is given in section IV followed by the references.

II. RELATED WORK

Image decomposition is, basically, the representation of the given grey or color image in different parts or components so that later, the original image can be recovered. Existing approaches in [1]-[8] are studied and the methodologies used are- Learning based decomposition and then denoising [1], learning based artifact removal [2], intrinsic decomposition [3]-[6], texture and cartoon decomposition [7] and weighted least squares-based approach [8]. Summary of the studied approaches in [1]-[8] is summarized in Table 1.

| Ref | Work Carried Out | Methodology | PEP | Dataset | Claim by author(s) | Our Findings |
|-----|---------------------------|-----------------------|----------------|-------------------|-------------------------|----------------------|
| [1] | Self-learning-based | Used sparse | PSNR | Rain images | Identified undesired | Unsupervised |
| | image decomposition | representation | | | noise patterns | clustering algorithm |
| [2] | Learning based | Bilateral filter, | Computational | Thorax & Pelvis | High image quality and | Enhanced the |
| | artefacts removal | dictionary learning, | cost | Phantom | low computational | performance with |
| | | sparse coding | | | complexity | less complexity |
| [3] | Image-space for | Per-pixel statistic & | RMSE, | MIT intrinsic | Computation of | No frame-by-frame |
| | estimating AO in image | photometric approach | average error, | image dataset | reflectance and | ordering or |
| | set | used | LMSE | | illumination without | coherence. |
| | | | | | smoothness | |
| [4] | IID for classification of | Feature extraction | Computational | Indian Pines, the | Higher classification | No implementation |
| | hyper spectral images | | time | University of | accuracy with small | of other hyper |
| | | | | Pavia, and | training samples | spectral |
| | | | | Salinas images | | applications |
| [5] | SSID for hyperspectral | SLIC & FH | Computational | Pavia dataset | Minimizes storage & | Failed to take |
| | images | | time | | computation | advantage of sparse |
| | | | | | requirements by using | constraints matrix |
| | | | | | superpixels | |
| [6] | Image fusion based on | Reflectance | Computational | Quickbird and | Seamlessly fused | Computational cost |
| | IID | prediction and | time | Worldview-2 | images without spectral | is higher |
| | | reflectance + PAN | | | distortion | |
| | | image | | | | |
| | | | | | | |

Table 1: Image Decomposition Techniques Summary

| [7] | Texture | Used BNN for | PSNR, SSIM | Berkeley | Handles blur + missing | Use of block wise |
|-----|------------------------|------------------|-------------|-------------------|------------------------|-------------------|
| | characterization-based | suitable | | segmentation | pixels images with | nature of BNN is |
| | image decomposition | characterization | | Database | different noise | challenging |
| [8] | Edge preserving image | Weighted Least | Application | Heart shaped | Feasible optimization | Method used in |
| | decomposition | Square (WLS) | Specific | cookies, Barbara, | framework | HDR tone mapping |
| | | | Metric | Girl, small | | |
| | | | | office, | | |

Image restoration means to restore the original grey or color image from the distorted or noisy grey or color image. In general, different techniques are used to restore the original image, namely, denoising, deblurring, etc. Existing approaches in [9]-[21] are studied and the methodologies used are- Echo state network and optimization [9], wavelet [10], Gaussian mixture model [11], group sparsity [12], neural network [13], patch based [14], scale map [15], auto encoder [16], gradient sparsity [17], adaptive norm selection [18], p-norm [19], group sparse [20], and tensor recovery [21]. Summary of the studied approaches in [9]-[21] is summarized in Table 2.

| Table 2: Image Restoration | Literature Summary |
|----------------------------|--------------------|
|----------------------------|--------------------|

| Ref | Work Carried Out | Methodology | PEP | Dataset | Claim by author(s) | Our Findings |
|------|---------------------------|----------------------|----------------|-------------------------------|--|------------------------------------|
| [9] | Differentiable error | Denoising-Based | SSIM, SSIM, | MIT-Adobe | Method can be acceptable | Choosing the |
| | function based on the | approach | MSSIM | FiveK Dataset | by visual inspection | right loss function |
| | performance of losses | | | | | is crucial |
| [10] | GSR using patches as | Self adaptive | PSNR, FSIM | Barbara, Boats, | Leverages both nonlocal | No solution for |
| | base | dictionary learning | | House, C. Man, | self-similarity and | image deblurring |
| | | | | Peppers, Lena | intrinsic local sparsity | in presence of |
| - | | | | | | impulse |
| [11] | Iterative denosing based | Off the shell | PSNR | Cameraman, | Utilizes fewer denoising | No high-quality |
| | image restoration | denoiser | | House, Lena, | NN for solving inverse | results and |
| | | | | Peppers, Barbara, | problems | computational |
| | | | | Boat, Hill, | | efficiency |
| | | | | Couple, | | |
| F101 | | 0 110 | DOND CODA | BSD68 | Estimation of each | Handles |
| [12] | Non-local extension of | Sparsity model of | PSNR, SSIM | Lena, Peppers, | | |
| | total variation (TV) | gradient image | | Airplane, Barbara, Fishing | gradient and adaptive learning of statistical | non-stationery nature on images |
| | regularization | | | boat, Sailboats | models | nature on images |
| [13] | Non-local variational | SS-based nonlocal | PSNR, SSIM | USC-SIPI image | Enhances the | Addresses the |
| [13] | technique based on SS | quadratic and total | 1 5141, 551141 | database | effectiveness of image | limitations of |
| | for image restoration | variation functions | | database | restoration with texture | intensity-based |
| | for mage restoration | (SS-NLH1 and | | | and structural information | patch distance |
| | | SS-NLTV) are used | | | und Stractural Information | puten distance |
| [14] | Determining the optimal | Adopts Piecewise | PSNR, | Cameraman, | Finds stable norm values | Failed to seek an |
| | norms for both fidelity | function and | Running | Barbera, Piret, | regardless of noise type | adaptive |
| | and regularization terms | regularize norms | Time | Peppers, Leaf, | C 11 | technique for |
| | - | | | Buildong, Aerial, | | determining an |
| | | | | Urban | | alternative in |
| | | | | | | regularization |
| [15] | Gradient distribution | Spatially variant | PSNR, SSIM | House, Peppers, | Achieving better quality | No need of |
| | based image restoration | hyper-Laplacian | | Lena, | and texture preservation | complex |
| | | distribution is used | | Boat | _ | parameter tuning |
| [16] | Autoencoder based | Auxiliary | PSNR, SSIM | Classic5 and | Incorporates | For multi-filters |
| | restoration for grayscale | variable technique | | LIVE1 dataset | higher-dimensional | either low rank |
| | images | | | | structural information and | regulation or |
| | | | | | enhances network | sparse |
| | | | | | stability. | representation is required |
| [17] | Frameworks using | Multispectral | PSNR | NIR & noisy | Effectively handles | Addresses the |
| [1/] | different inputs like NIR | shadow detection is | FONK | color images | structural divergence and | issues of |
| | image and noisy color | used | | color images | achieves visually plausible | |
| | image and horsy color | useu | | | image reconstruction. | image restoration |
| [18] | RNN based ESN for | Neurodynamic | PSNR, MSE, | Judd and Torallba | Enhances the capabilities | Finding the |
| [10] | restoring image | Optimization | NRMSE | dataset | of ESNs for effectively | optimal |
| | BB. | approach based on | | | recovering high-quality | parameter is still a |
| | | RNN | | | images from degraded or | big challenge |
| | | | | | noisy versions. | 6 |
| [19] | Restoring images by | An edge-driven | PSNR, | Slope, Angry | Handles the estimation of | Unsuitable for |
| | representing them as | wavelet frame model | Datagram | Birds, Peppers, | image singularities and | images with |

| | piecewise smooth | is used | Loss Rate | Sonic, | offers improved | texture |
|------|---------------------|---------------------|-------------|-------------------|--------------------------|-------------------|
| | functions | | | Train, Airplane, | regularization | |
| | | | | Oil Painting, and | | |
| | | | | Pitt | | |
| [20] | Wavelet frame-based | Treating the images | SSIM | Car, | Restores images by | Hindering the |
| | image restoration | as a piecewise | | Goldengate, | preserving singularities | guarantee of both |
| | | smooth function | | Interior, Pitt, | | edges and |
| | | | | Samantha | | sharpness. |
| [21] | Minimize the | Blind deconvolution | Computation | Debris Images | Minimizes expensive | Struggle to store |
| | consequence of blur | method | Cost | | computations and | fine textures |
| | | | | | improvement in debris | |
| | | | | | analysis | |

III. FORMULATION OF PROBLEM AND PROPOSED APPROACH

In general, it is found that the filtering banks can be used to decompose the images. In view of the development of the proposed filtering-based color image decomposition approach to address the issue of color image restoration, the baseline problem is formulated as follows:

Consider the color image I is firstly separated as the grey images (R-plane, G-plane and B-plane grey level images). That is,

 $R = \{Intensity values from 0-255\},\$

 $G = \{Intensity values from 0-255\},\$

 $B = \{Intensity values from 0-255\},\$

 $I = \{R, G, B\}$

Later, each grey level plane is degraded with some noise η to get the degraded grey level plane images.

 R_D - Degraded R-plane with the insertion of noise η .

 G_D - Degraded G-plane with the insertion of noise η .

 B_D - Degraded B-plane with the insertion of noise η .

Then these each degraded grey level planes (R_D , G_D , and B_D) are decomposed into three components in view of the color image restoration.

 R_D - Decomposed into R_D - C_1 , R_D - C_2 , and R_D - C_3 .

 G_D - Decomposed into G_D - C_1 , G_D - C_2 , and G_D - C_3 .

 B_D - Decomposed into B_D - C_1 , B_D - C_2 , and B_D - C_3 .

These three decomposed components (C_1, C_2, C_3) for each grey level plane can be obtained by using the combination of different filters or by using the typical filters

 $F(\cdot)$ (*i.e.*, average filter, median filter, max filter, min filter, etc.). It is a matter of investigation to identify the particular filter which should be used only once or the filter banks or the combination of filters as shown in



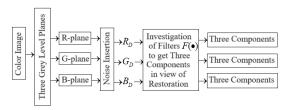


Figure 1: Filtering based Image Decomposition

Then these each degraded grey level planes (R_D , G_D , and B_D) are decomposed into three components in view of the color image restoration.

Being the proposed image restoration approach is based on the image decomposition and that is related to the filtering-based image decomposition, so, due consideration should be given to the noise percentage in the generated/decomposed three components of the degraded grey level plane images. And, later the development of the denoising/restoration mechanism to reconstruct the original color image by reconstructing grey level plane images. Reconstructed color image I can be restored through the flow given in Figure 2.

By referring the presented problem formulation of image restoration based on image decomposition, one can investigate different filters from the image decomposition point of view. Various types of approaches can be developed based on filtering. It can be work out by using homogeneous or heterogeneous filters (e.g. simple average or median filters or the combination of average and median filters). If the original image is not distorted then the original image is degraded with the insertion of noise. And, then it is decomposed into three components. As these three components involves the noise, so it is necessary to evaluate the percentage of noise in these three components. Noise percentage evaluation may involve the use of variance and standard deviation. Finally, once done with the noise percentage evaluation, one can design the denoising mechanism to remove the noise in components to recover the noise free components which in turn produces the corresponding grey image or grey level plane of the color image. Reconstructed color planes can be combined to get the reconstructed color image.

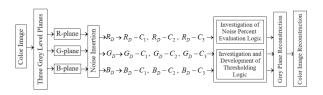


Figure 2: Decomposition based Image Restoration

IV. CONCLUSION

This paper discussed about the possible image decomposition and image restoration mechanisms or approaches. Different type of image decomposition approaches is possible and hence different type of image restoration approaches are possible. This paper is useful for the beginners in the domain of the image decomposition and image restoration.

REFERENCES

- D. -A. Huang, L. -W. Kang, Y. -C. F. Wang and C. -W. Lin, "Self-Learning Based Image Decomposition with Applications to Single Image Denoising," in IEEE Transactions on Multimedia, vol. 16, no. 1, pp. 83-93, Jan. 2014. https://doi.org/10.1109/TMM.2013.2284759.
- [2] X.-Y. Cui, Z.-G. Gui, Q. Zhang, H. Shangguan and A. -H. Wang, "Learning-Based Artifact Removal via Image Decomposition for Low-Dose CT Image Processing," in IEEE Transactions on Nuclear Science, vol. 63, no. 3, pp. 1860-1873, June 2016. https://doi.org/10.1109/TNS.2016.2565604.
- [3] D. Hauagge, S. Wehrwein, K. Bala and N. Snavely, "Photometric Ambient Occlusion for Intrinsic Image Decomposition," in IEEE Transactions on Pattern Analysis and Machine Intelligence, vol. 38, no. 4, pp. 639-651, 1 April 2016. https://doi.org/10.1109/TPAMI.2015.2453959.
- [4] X. Kang, S. Li, L. Fang and J. A. Benediktsson, "Intrinsic Image Decomposition for Feature Extraction of Hyperspectral Images," in IEEE Transactions on Geoscience and Remote Sensing, vol. 53, no. 4, pp. 2241-2253, April 2015. https://doi.org/10.1109/TGRS.2014.2358615.
- [5] X. Jin and Y. Gu, "Superpixel-Based Intrinsic Image Decomposition of Hyperspectral Images," in IEEE Transactions on Geoscience and Remote Sensing, vol. 55, no. 8, pp. 4285-4295, Aug. 2017. https://doi.org/10.1109/TGRS.2017.2690445.
- [6] Kang, X., Li, S., Fang, L. et al. Pansharpening Based on Intrinsic Image Decomposition. Sens Imaging 15, 94 (2014). https://doi.org/10.1007/s11220-014-0094-8
- [7] S. Ono, T. Miyata and I. Yamada, "Cartoon-Texture Image Decomposition Using Blockwise Low-Rank Texture Characterization," in IEEE Transactions on Image Processing, vol. 23, no. 3, pp. 1128-1142, March 2014. https://doi.org/10.1109/TIP.2014.2299067.

- [8] Shao, P., Ding, S., Ma, L. et al. Edge-preserving image decomposition via joint weighted least squares. Comp. Visual Media 1, 37–47 (2015). https://doi.org/10.1007/s41095-015-0006-4
- [9] H. Duan and X. Wang, "Echo State Networks With Orthogonal Pigeon-Inspired Optimization for Image Restoration," in IEEE Transactions on Neural Networks and Learning Systems, vol. 27, no. 11, pp. 2413-2425, Nov. 2016, https://doi.org/10.1109/TNNLS.2015.2479117.
- [10] Jian-Feng Cai, Bin Dong, Zuowei Shen, Image restoration: A wavelet frame based model for piecewise smooth functions and beyond, Applied and Computational Harmonic Analysis, Volume 41, Issue 1, 2016, Pages 94-138, ISSN 1063-5203. https://doi.org/10.1016/j.acha.2015.06.009.
- [11] M. Niknejad, H. Rabbani and M. Babaie-Zadeh, "Image Restoration Using Gaussian Mixture Models With Spatially Constrained Patch Clustering," in IEEE Transactions on Image Processing, vol. 24, no. 11, pp. 3624-3636, Nov. 2015. https://doi.org/10.1109/TIP.2015.2447836.
- [12] Jun Liu, Ting-Zhu Huang, Ivan W. Selesnick, Xiao-Guang Lv, and Po-Yu Chen. 2015. Image restoration using total variation with overlapping group sparsity. Inf. Sci. 295, C (February 2015), 232–246. https://doi.org/10.1016/j.ins.2014.10.041
- [13] H. Zhao, O. Gallo, I. Frosio and J. Kautz, "Loss Functions for Image Restoration With Neural Networks," in IEEE Transactions on Computational Imaging, vol. 3, no. 1, pp. 47-57, March 2017. https://doi.org/10.1109/TCI.2016.2644865.
- [14] V. Papyan and M. Elad, "Multi-Scale Patch-Based Image Restoration," in IEEE Transactions on Image Processing, vol. 25, no. 1, pp. 249-261, Jan. 2016. https://doi.org/10.1109/TIP.2015.2499698.
- [15] Xiaoyong Shen, Qiong Yan, Li Xu, Lizhuang Ma, and Jiaya Jia. 2015. Multispectral Joint Image Restoration via Optimizing a Scale Map. IEEE Trans. Pattern Anal. Mach. Intell. 37, 12 (Dec. 2015), 2518–2530. https://doi.org/10.1109/TPAMI.2015.2417569
- [16] Ruxin Wang and Dacheng Tao. 2016. Non-Local Auto-Encoder With Collaborative Stabilization for Image Restoration. Trans. Img. Proc. 25, 5 (May 2016), 2117–2129. https://doi.org/10.1109/TIP.2016.2541318
- [17] H. Liu, R. Xiong, X. Zhang, Y. Zhang, S. Ma and W. Gao, "Nonlocal Gradient Sparsity Regularization for Image Restoration," in IEEE Transactions on Circuits and Systems for Video Technology, vol. 27, no. 9, pp. 1909-1921, Sept. 2017. https://doi.org/10.1109/TCSVT.2016.2556498.
- [18] H. Shen, L. Peng, L. Yue, Q. Yuan and L. Zhang, "Adaptive Norm Selection for Regularized Image Restoration and Super-Resolution," in IEEE Transactions on Cybernetics, vol. 46, no. 6, pp.

1388-1399, June 2016. https://doi.org/10.1109/TCYB.2015.2446755.

- [19] Y. Xie, Y. Qu, D. Tao, W. Wu, Q. Yuan and W. Zhang, "Hyperspectral Image Restoration via Iteratively Regularized Weighted Schatten p-Norm Minimization," in IEEE Transactions on Geoscience and Remote Sensing, vol. 54, no. 8, pp. 4642-4659, Aug. 2016. https://doi.org/10.1109/TGRS.2016.2547879.
- [20] J. Zhang, D. Zhao and W. Gao, "Group-Based Sparse Representation for Image Restoration," in IEEE

 Transactions on Image Processing, vol. 23, no. 8, pp.

 3336-3351,
 Aug.
 2014.

 https://doi.org/10.1109/TIP.2014.2323127.
 2014.

[21] H. Fan, Y. Chen, Y. Guo, H. Zhang and G. Kuang, "Hyperspectral Image Restoration Using Low-Rank Tensor Recovery," in IEEE Journal of Selected Topics in Applied Earth Observations and Remote Sensing, vol. 10, no. 10, pp. 4589-4604, Oct. 2017. https://doi.org/10.1109/JSTARS.2017.2714338.

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